du niobium pur puisque les distances Nb–Nb sont normalement supérieures à 2,5 Å (2,54 Å dans Nb₃Si₃ β) dans ces types d'alliages.

Ces distances métal—métal (2,48 Å) de la structure de Nb₇₈Fe₄₀Si₈₀ sont par ailleurs très voisines de celles caractérisant les chaînes Fe—Fe de Nb₄Fe₄Si₇ (2,49 Å) ou Cr—Cr de Nb₄CrSi₃ (2,47 Å).

Donc, à partir d'une occupation des sites Fe(3) et Fe(6) en fer pur, correspondant à la formule $Nb_{76}Fe_{42}$ -Si₈₀ l'alliage au niobium doit être limité et le domaine d'homogénéité ne s'étend pas bien au-delà de la composition des cristaux analysés, comme le confirment les résultats de l'étude cristallographique sur poudres, et la deuxième composition limites $Nb_{80}Fe_{38}$ -Si₈₀, doit correspondre pour les deux sites concernés par les substitutions Nb–Fe à un taux d'alliage d'environ 50%.

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Hydrogen Bonding in MgHPO₄. 3H₂O (Newberyite)

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Abstract

The structure of pure synthetic crystals of MgH-PO₄. $3H_2O$ (newberyite) [a = 10.203 (3), b = 10.678 (4), c = 10.015 (3) Å, Z = 8, space group *Pbca*] was refined to R = 0.047 for 1137 non-zero reflections measured on an automatic diffractometer with Cu $K\alpha$ radiation. All H atoms were located on a difference map and included in the refinement. The structure can be described as layers parallel to (010), built up by Mg octahedra sandwiched between phosphate tetrahedra, both running along [001]. These layers are only connected by hydrogen bonds involving the water molecules. The hydrogen-bond system is discussed and the functions of the different water molecules are described. One of them forms a bifurcated hydrogen bond.

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Introduction

MgHPO₄.3H₂O is found as a mineral (newberyite) and as a constituent of human and animal calculi. The significance of its presence in human urinary stones is still controversial: the question is whether newberyite has its primary origin in stones or, as is more probable, it is a decomposition product of struvite (MgNH₄-PO₄.6H₂O), with which it is usually associated (Sücker, 1963; Sutor, 1968; Whitaker, 1968). In felines, on the contrary, newberyite appears to be deposited as such (Sutor, Wooley & Jackson, 1970).

The crystal structure of newberyite, as regards the heavy atoms, was determined by Sutor (1967) on a small elongated fragment of natural crystal from Skipton Caves (Victoria, Australia), but no attempt was made to locate the H atoms; nevertheless some hydrogen bonds were suggested on the basis of $O \cdots O$ contacts.

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In our research programme on calculi growth, we are investigating the structural and genetic relationships between struvite and other crystalline components of calculi, among them newberyite. That implies knowledge of the surface structure of many crystal faces and the characterization of the bond system in the structure; for newberyite, therefore, the exact localization of the H atoms is of prime importance.

As large single crystals of newbervite were obtainable, we succeeded in locating the H atoms by X-ray methods. We present here the results of our work, which has been carried out on synthetic pure crystals, with a discussion of the hydrogen-bond system; the work also represents a contribution to the crystal chemistry of acidic magnesium orthophosphates.

Experimental

Synthetic crystals of newbervite can be obtained by a variety of methods (De Schulten, 1903). By a new method, which involves mixing aqueous solutions of magnesium chloride or sulphate with ammonium dihydrogenphosphate at 310 K, and adjusting the pH to about 5.5 with ammonium hydroxide, we prepared large colourless pseudo-octahedral single crystals. The crystal habit is characterized by the large development of the {111} bipyramid, and by the occurrence of small or very small faces belonging to the forms $\{100\}$, $\{010\}, \{101\} \text{ and } \{102\}.$

Weissenberg and precession photographs and singlecrystal diffractometry confirmed orthorhombic symmetry with space group *Pbca*. Cell parameters [a =10.203(3), b = 10.678(4), c = 10.015(3) Å] were obtained by least squares from 25 centred reflections, measured on a diffractometer (Cu $K\alpha$ radiation). They are in excellent agreement with those measured using very pure crystals from Mono Lake (California), but smaller than those of impure crystals from Skipton Caves (Australia), where 0.36 wt.% Mn probably replaces Mg (Cohen & Ribbe, 1966; Sutor, 1967); a is more sensitive to the replacement than the other two cell constants.

Other data are: Z = 8, $V = 1091 \cdot 11$ Å³, $M_r = 174 \cdot 34$, $D_o = 2 \cdot 123$ (De Schulten, 1903), $D_c = 2 \cdot 122$ Mg m⁻³, F(000) = 720, $\mu(Cu K\alpha) = 5.5 \text{ mm}^{-1}$.

The crystal used for data collection was shaped into a sphere of 0.4 mm diameter. The intensities were collected on an Enraf-Nonius CAD-4 diffractometer with the θ -2 θ scan mode, a scan width of 0.9° and a scan speed of 2° min⁻¹. Cu K α radiation with a Ni filter was used to record reflections up to $2\theta = 175^{\circ}$. 2450 reflections (hkl and hkl) were measured. A periodic check of several standard reflections showed no significant intensity variation. Equivalent intensities were merged into a set of 1230 independent reflections. The internal consistency index $R_I = \sum (I - \overline{I}) / \sum I$, where \overline{I} is the weighted mean of *hkl* and *hkl* intensities, was 3.6%.

All data were corrected for absorption (sphere approximation), Lorentz and polarization effects. The e.s.d. of each intensity, $\sigma(I)$, was calculated according to the method of Stout & Jensen (1968). On the basis of a $2\sigma(I)$ test, 1137 reflections were considered observed. Scattering factors are from Moore (1963). Real and imaginary dispersion corrections were applied for P and Mg (Cromer & Waber, 1974).

Refinement

Refinement was started with atomic parameters reported by Sutor (1967). The initial $R = (\sum ||F_o|| |F_c|| / \sum |F_c| = 0.11$. During these calculations we observed that the strongest reflections were significantly affected by secondary extinction. We excluded these from the refinement and Fourier syntheses. In the final structure factor calculation these intensities were corrected, according to $I_{\text{corr}}/I_{\text{obs}} = k(1 + 2gI_{\text{corr}})$. k and g, determined by least squares from the plot, are respectively 1.02 and $3 \times 10^{-5} e^{-2}$. Full-matrix least-squares refinement was based on F and the function minimized was $\sum w(|F_o| - |F_c|)^2$, where $w(F) = 1/\sigma^2(F)$. For the nine non-hydrogen atoms, which were assigned anisotropic thermal parameters, the refinement converged to R = 0.056 and $R_w = 0.065$. At this stage a difference map revealed the positions of the seven H atoms. Further refinement was carried out with H atoms included, their positional and isotropic thermal parameters being varied simultaneously with all the nonhydrogen atom parameters. The final R was 0.047 $(R_w = 0.060)$ and 0.058 for all observed data (strong intensities corrected for secondary extinction); a dif-

Table 1. Fractional atomic coordinates $(\times 10^4; for$ $H \times 10^3$) with significant figures of the e.s.d.'s in parentheses

	x	у	Z
Р	-89.9 (7)	1328.7 (7)	1537-2 (8)
Mg	2969.4 (9)	2466.3 (9)	862.0 (9)
O(3)	-884 (3)	1996 (2)	2578 (3)
O(4)	-514(2)	1617 (2)	98 (2)
O(5)	1392 (2)	1535 (2)	1681 (2)
O(6)	-341(3)	-128(2)	1783 (3)
W(7)	1671 (3)	3129 (3)	-614 (3)
W(8)	2500 (3)	4125 (3)	1894 (3)
W(9)	3539 (3)	924 (3)	-319 (3)
H(1)	174 (5)	310 (5)	-161 (5)
H(2)	80 (5)	290 (4)	-53 (4)
H(3)	278 (5)	485 (5)	167 (5)
H(4)	175 (4)	429 (4)	232 (4)
H(5)	313 (8)	88 (8)	-97 (8)
H(6)	351 (5)	-4 (5)	-4 (6)
H(7)	-16(6)	-62 (7)	98 (6)

ference map was now featureless. Final positional parameters are given in Table 1.*

Description and discussion of the structure

Coordination polyhedra

The P–O and O–O distances and O–P–O angles within the phosphate tetrahedron are given in Table 2 or in Fig. 1; for clarity the atom numbering is the same as that of Sutor (1967), except for the O atoms of water molecules which are indicated as W. Our values are very close to those found by Sutor (1967). The three distortion indices (Baur, 1974) for the P-O and O-O distances and the O-P-O angles (0.018, 0.0076, 0.029, respectively) correspond to the average values for acidic orthophosphates (0.017, 0.011, 0.025, respectively).

* Lists of structure factors and thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 34603 (10 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.



Fig. 1. Hydrogen bonding of H(7) between the centrosymmetrically related PO₄ groups (+ denotes the centre of symmetry).

Table	2.	Interatomic	distances	(A)	and	O-P-O
		angles (°) v	<i>vithin the</i> P	O₄gr	оир	

The e.s.d.'s are 0.002 and 0.003 Å for the P-O and O-O distances respectively and 0.1° for the angles.

P-O(3)	1.500	P-O(5)	1.535		
P-O(4)	1.536 Average	PO(6) 1-542	1.596		
O(3) - O(4)	2.544	O(4)–O(5)	2.511		
O(3)–O(5)	2.538	O(4)–O(6)	2.520		
O(3)–O(6)	2.467	O(5)–O(6)	2.509		
	Average	2.515			
O(3)-P-O(4)	113-8	O(4)–P–O(5)	109.7		
O(3) - P - O(5)	113.5	O(4) - P - O(6)	107.1		
O(3)-P-O(6)	105.6	O(5)–P–O(6)	106.5		
	Average	110.4			

Even the Mg–O and O–O distances and the angles O-Mg-O within the Mg octahedron (Table 3, Fig. 2)* are very close to those reported by Sutor (1967); the difference between the average values is 0.24%.

Hydrogen bonding

The geometrical features of the H bonds are shown in Table 4; distances and angles involving the H atoms are satisfactory, taking into account that X-ray diffraction shortens the O-H distance. The acidic H(7)atom is attached to O(6), as Sutor (1967) suggested, and forms a H bond with O(4.2),* which is 1.67 Å

^{*} Atoms are labelled as follows: a single number (or no number) denotes an atom of the asymmetric unit; a second number, ranging from 2 to 8, indicates positions: (2) $\bar{x}, \bar{y}, \bar{z}$; (3, 4) $\pm (\frac{1}{2} + x, \frac{1}{2} - y, \bar{z})$; $(5, 6) \pm (\bar{x}, \frac{1}{2} + y, \frac{1}{2} - z); (7, 8) \pm (\frac{1}{2} - x, \bar{y}, \frac{1}{2} + z).$ Translations are represented by Roman numbers: (I) -c; (II) -b.



Fig. 2. Projection along [010] showing the Mg-atom environment.

Table 3. Interatomic distances (Å) and O-Mg-O angles (°) in the Mg coordination polyhedron

The e.s.d.'s are 0.002 and 0.003 Å for Mg–O and O–O distances, respectively, and 0.1° for the angles.

Mg-O(3,8)	2.015	O(3,8) - Mg - W(8)	87.8
Mg = O(4,3)	2.068	O(3,8) - Mg - W(9)	94.6
Mg-O(5)	2.062	O(3,8) - Mg - O(5)	91.4
Mg - W(7)	2.107	O(3,8) - Mg - O(4,3)	92.6
Mg - W(8)	2.106	W(7)-Mg-O(5)	87.2
Mg - W(9)	2.109	W(7) - Mg - W(9)	92.4
Average	2.078	W(7) - Mg - W(8)	85.3
U		W(7) - Mg - O(4,3)	89.1
O(3,8) - W(8)	2.858	W(8) - Mg - O(5)	91.9
O(3,8) - W(9)	3.032	W(8) - Mg - O(4,3)	90.0
O(3.8) - O(5)	2.918	W(9) - Mg - O(5)	93.5
O(3.8) - O(4.3)	2.952	W(9) - Mg - O(4,3)	84.4
W(7) - O(5)	2.875	Average	90.0
W(7) - W(9)	3.043	C	
W(7) - W(8)	2.856	O(5) - Mg - O(4,3)	175.7
W(7) - O(4,3)	2.930	W(7) - Mg - O(3,8)	172.9
W(8) - O(5)	2.995	W(8) - Mg - W(9)	174.0
W(8) - O(4,3)	2.953		
W(9) - O(5)	3.039		
W(9) - O(4,3)	2.807		
Average	2.938		

Average

distant from H(7). This H bond, which deviates significantly from linearity $[O(6)-H(7)\cdots O(4,2) = 162^{\circ}]$, is the strongest H bond in the structure, and corresponds to the typical distance for this kind of bond, 2.615 Å (Fig. 1).

As expected, the largest P–O distance within the PO₄ group corresponds to the short H–O bond. All the H atoms of water molecules are engaged in H bonds of different strengths; W(7) and W(8) form H bonds only with O atoms of the PO₄ group, whereas W(9) is hydrogen bonded only to O atoms of the water molecules. $W \cdots W$ contacts range from 2.986 to 3.118 Å, indicating weak H bonds, while the O–W contacts range from 2.690 to 2.845 Å corresponding to medium-strong hydrogen bonds.

Besides the two H bonds shown in Table 4, W(7) is connected to O(3,3) by H(1) [H(1) \cdots O(3,3) = 2.611 Å] but this contact cannot be considered as a H bond, since H(1) is already engaged in a strong H bond with O(5,6)^I. Moreover O(3,3) \cdots H(1) $-W(7) = 116^{\circ}$ is too far from the linearity condition and normal geometry of a water molecule (Ferraris & Franchini-Angela, 1972).

W(8) forms two H bonds, one for each H atom: H(3) to O(5,4) ($W \cdots O = 2.819$ Å) and H(4) to O(6,5) ($W \cdots O = 2.690$ Å). H(3) is also in close contact with O(6,4) and W(9,4) at 2.616 and 2.652 Å respectively; even if the $W \cdots O$ distances are acceptable for H bonds [$W(8) \cdots O(6,4) = 3.009$; $W(8) \cdots W(9,4) =$ 3.118 Å], the contacts cannot be considered as H bonds, since the corresponding donor-H-acceptor angles are 108 and 114°, respectively. Moreover O(6,4) and W(9,4) are 1.40 and 2.33 Å out of the water-molecule plane.

The water molecule W(9) is near three water molecules, $W(7,4)^{II}$, $W(8,4)^{II}$ and $W(8,6)^{I}$, at similar distances, $W(9) \cdots W(8,6)^{I} = 2 \cdot 986$, $W(9) \cdots W(7,4)^{II} = 3 \cdot 007$, $W(9) \cdots W(8,4)^{II} = 3 \cdot 118$ Å; with the first, $W(8,6)^{I}$, H(5) forms one H bond. As the distances H(6) $\cdots W(7,4)^{II}$ and H(6) $\cdots W(8,4)^{II}$ are smaller than 2 \cdot 4 Å, the sum of the corresponding van der Waals radii, H(6) is thought to form a bifurcated H bond of approximately the same strength with each of these two water molecules, even though one of them is quite out of the W(9) plane $[W(7,4)^{II}$ is 0 · 44 and $W(8,4)^{II}$ 1 · 73 Å from the plane, with W(9)-H(6) $\cdots W(7,4)^{II}$ = 148 and W(9)-H(6) $\cdots W(8,4)^{II}$ = 126°].

The H-bond system found in newberyite excludes the possibility, suggested by Sutor (1967), of H bonds within the Mg octahedron.

CaHAsO₄. $3H_2O$ is isostructural with newberyite (Catti & Ferraris, 1973). The H bonding involving W(7) and W(8) is the same as that of W(3) and W(1), respectively, in CaHAsO₄. $3H_2O$. An anomaly occurs in the third water molecule, W(9) in newberyite and W(2) in the arsenate: whereas H(5) in newberyite forms a H bond with $W(8,6)^1$, in the arsenate the corresponding H(5) atom is thought to be almost free from H bonding; the other H atom in newberyite, H(6), forms a bifurcated H bond, while the corresponding H atom in the arsenate, H(4), forms a single H bond.

Crystal packing

The structure consists of alternating P and Mg strata parallel to (100) (Sutor, 1967), but it may be also described in terms of (010) layers (Fig. 3). These layers are built up by Mg octahedra sandwiched between phosphate tetrahedra, running along [001]. Three O atoms of each PO₄ tetrahedron are nearly parallel to (010), whereas the fourth points up and down alternately along [001]. Within the (010) layer the three O atoms of the PO₄ group are connected along [100] and [001] to as many Mg atoms forming a network of strong bonds. Additional interactions in the (010) plane are provided by H bonds between the water molecules and the O atoms in the [100] and [001] directions. Between the (010) layers only H bonds are established. because of the different roles of water molecules. W(7)forms its H bonds within the (010) layer, connecting the polyhedra along [100] and [001]. W(8) ties one Mg octahedron of the layer to two PO4 groups of the facing layer, whereas W(9) forms one of its H bonds within the (010) Mg octahedra of the facing layer.

Electrostatic balance

Bond-strength values were obtained by applying the universal third-row relationship $s = (R/1.622)^{-4.29}$ (Brown & Shannon, 1973) for P–O and Mg–O bonds and the *s versus* O···O distance curve (Brown, 1976) for H bonds; the results are summarized in Table 5.

Table 4. Interatomic distances (Å) and angles (°) in hydrogen bonds

The e.s.d.'s are 0.05 Å and 5° for distances and angles involving H atoms.

AB	BC	AC	ABC	A	B	С	D	Ε	CE	CD	DE	CDE	BCD
1.794	1.00	2.747	158	O(5,6) ¹	···H(1)	-W(7)	H(2)····	O(4)	2.845	0.93	2.01	148	98
1.963	0.88	2.819	164	O(5,4)·	··H(3)-	-W(8)-	-H(4)····	O(6,5)	2.690	0.89	1.80	171	102
2.229	0.78	2.986	164	W(8,6) ¹	····H(5)-W(9))-H(6) 🕻	$\cdot W(7,4)^{I}$ $\cdot W(8,4)^{I}$	□ 3.007 □ 3.118	1.07 1.07	2·04 2·37	148 125	98
					P-C	D(6)–H	(7)···O(4,2)	2.615	0.98	1.67	162	111



Table 5. Electrostatic balance



Fig. 3. Hydrogen-bond network in newberyite; projection along [010].

The electrostatic balance for O atoms corresponds to the expected values according to the Pauling rules except for O(3) and W(9), which are underbonded ($s_i =$ 1.80) and overbonded ($s_i = 2.18$) respectively. The P-O(3) distance (1.500 Å) is one of the shortest found in orthophosphate groups. The underbonding of the O atom, which is usually observed in these cases, suggests some limited validity of Brown & Shannon's formula for short or very short bond distances. O(3) is the only O atom which is not an acceptor of a H bond; it has the strongest bond with P and Mg.

The difference in bond distances between Mg–O (average: 2.048 Å) and Mg–W (average: 2.107 Å) (Table 3) is due to the underbonding of O atoms [especially O(3)], which demands an approach of these atoms to the P and Mg atoms with respect to the water molecules, which exchange a small bond valence through their generally long H bonds.

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The Structure of Potassium Tantalum Fluoride Oxide K₁₂Ta_{15'5}F_{18'5}O_{35'5}

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Abstract

The structure of $K_{12}Ta_{15.5}F_{18.5}O_{35.5}$ has been determined and refined in space group P6 to an R of 0.063. 0567-7408/79/112518-05\$01.00 It can be described as a three-dimensional framework formed by the interpenetration of two distinct sublattices with the formulations $[Ta_5X_{17}]_{3n}$ and $[Ta_{0.5}X_3]_n$ (X =O, F). The $[Ta_5X_{17}]_{3n}$ skeleton is formed entirely of © 1979 International Union of Crystallography